

## Econometric Analysis of Monthly Peak-Hour and Total Usage Patterns of Hong Kong's Cross-Harbor Tunnels

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1 **An Econometric Analysis of Monthly Peak-Hour and Total Usage Patterns of Hong Kong's**  
2 **Cross-Harbor Tunnels**

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**ABSTRACT**

As one of the most densely populated metropolises in the world, Hong Kong daily sees severe traffic delays at the Cross-Harbour Tunnel (CHT), though not at the Eastern Harbour Crossing (EHC) and the Western Harbour Crossing (WHC). In 2013, the Hong Kong Special Administrative Region (HKSAR) Government proposed raising the tolls of the publicly-owned CHT and lowering those of the publicly-owned EHC for nine vehicle types: private cars, motorcycles, taxis, three kinds of buses, and three kinds of goods vehicles. The privately-owned WHC's already high tolls, however, would remain unchanged. Using monthly usage and peak-hour usage data for January 2003 through June 2015, we estimate a Generalized Leontief demand system to find that private cars, motorcycles and goods vehicles have price-sensitive tunnel usage patterns that are also time-dependent. The usage patterns of taxis and buses, which are public transportation vehicles, are totally price-insensitive. These findings suggest that the HKSAR Government's proposed toll changes would reduce the CHT's monthly usage by 7.4% to 12.2%, and peak-hour usage 5.0% to 16.8%. These usage reduction estimates suggest that a time-of-use (TOU) toll design can better manage CHT congestion than the current non-TOU design.

*Keywords:* Congestion Pricing, Transportation demand, Traffic management

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## 1 INTRODUCTION

2 Efficient rationing of the use of congestible roads, bridges, and tunnels is an important aspect of  
3 transportation policy (1-7). Like their counterparts in other Chinese metropolises (e.g., Beijing,  
4 Shanghai, Guangzhou and Shenzhen), Hong Kong drivers encounter severe traffic congestion on a  
5 daily basis, reflecting that Hong Kong is one of the most densely populated cities in the world.  
6 Encompassing an area of  $\sim 1100 \text{ km}^2$  ( $1 \text{ mi}^2 = 2.59 \text{ km}^2$ ), Hong Kong has a population of  $\sim 7.3$   
7 million, resulting in a high population density of  $\sim 6636$  residents per  $\text{km}^2$ . It has about 340  
8 licensed vehicles for every km ( $1 \text{ mi} = 1.62 \text{ km}$ ) of road and would become one big parking lot if  
9 most of these vehicles were on the road at the same time.

10 This paper is an econometric analysis of the effectiveness of the Hong Kong Special  
11 Administrative Region (HKSAR) Government's 2013 proposal to change the tolls of Hong  
12 Kong's three cross-harbor tunnels: the dual 2-lane Cross-Harbour Tunnel (CHT), the dual 2-lane  
13 Eastern Harbour Crossing (EHC), and the dual 3-lane Western Harbour Crossing (WHC); see  
14 Figure 1. Despite an excellent public transportation system that serves about 12.5 million  
15 passenger-trips per day, Hong Kong daily sees severe traffic delays between 07:00 and 21:00 at the  
16 CHT. A cross-harbor vehicular trip via the 1.8 km CHT may take up to 30 minutes, thanks to long  
17 queues along the roads leading to the CHT's northern end in Kowloon Peninsula and southern end  
18 on Hong Kong Island. The same trip, however, can be completed in about six minutes ( $= 1.8 \text{ km}$   
19  $\text{distance} \div \text{vehicle speed of } \sim 20 \text{ km per hour}$ ) during the uncongested hours (e.g., 02:00 to 06:00).

20 Figure 2 shows that the CHT's aggregate usage per day is about 120,000 vehicular trips in  
21 both directions, far above the design capacity of 78,000 trips under uncongested conditions. In  
22 contrast, the EHC's aggregate usage per day is below the design capacity of 78,000 trips and the  
23 WHC's is less than one third of the design capacity of 180,000 trips. The CHT's heavy congestion  
24 is understandable, thanks to the CHT's central location as shown in Figure 1, and the low monthly  
25 average tolls shown in Figure 3.

26 The proposed toll changes aim to price-manage the tunnel usage patterns of nine vehicle  
27 types: private cars, taxis, motorcycles, three kinds of buses, and three kinds of goods vehicles (9).  
28 If implemented, the proposal would raise the vehicle-specific tolls of the publicly-owned CHT and  
29 lower those of the publicly-owned EHC, while keeping those of the privately owned WHC  
30 unchanged. Our econometric evidence is timely and relevant, underscored by the HKSAR  
31 Government's initiation in late 2015 of a three-month public consultation on an electronic  
32 road-pricing pilot for the highly congested Central district and adjacent areas (10).

33 Our paper is motivated by a presumption of price-sensitive tunnel usage patterns by vehicle  
34 type, which implies that the proposed toll changes would shift some traffic away from the heavily  
35 congested CHT to the uncongested EHC and WHC (see Figure 1). While this presumption seems  
36 reasonable in light of the extant studies of Hong Kong's cross-harbor tunnel demands (11-13), a  
37 critical but unanswered question remains: can the same proposal alter each tunnel's peak-hour  
38 usage as measured by the maximum number of vehicular trips in a single hour of a given month? If  
39 the answer is "no", the proposal's effectiveness in price-managing the CHT's time-dependent  
40 congestion is very much in doubt. Hence, our joint investigation of the three tunnels' monthly  
41 peak-hour and total usage patterns sharply differentiates this paper from (11-13).

42 We answer the above question using the monthly cross-harbor tunnel usage data for the  
43 150-month period of January 2003 to June 2015 from the Hong Kong Transportation Department.  
44 We estimate the vehicle-specific disaggregate own- and cross-price elasticities of monthly  
45 peak-hour and total usage by tunnel and direction (northbound vs. southbound). These  
46 disaggregated elasticity estimates are then used to develop each tunnel's aggregate price elasticity  
47 estimates. Finally, we estimate the changes in each tunnel's peak-hour usage by direction, thereby

1 addressing the CHT's time-dependent congestion problem.

2 Our paper makes three contributions to Hong Kong's policy debates on cross-harbor tunnel  
3 congestion and the broader literature on transportation demand management. First, it presents an  
4 approach of system demand estimation that uses publicly available data to dissect a complicated  
5 real-world peak-hour congestion problem involving nine vehicle types, three tunnels, and two  
6 directions. The approach is useful when survey data collection is costly but aggregate data are  
7 readily available (14), yielding results that might complement empirical findings based on  
8 route-choice survey data (e.g., 12, 15-18). Second, our paper documents that the price-sensitivity  
9 of tunnel usage patterns is both time- and direction-dependent. As a result, the HKSAR  
10 Government's proposed toll changes represent a first step in price-managing the CHT's severe  
11 congestion. A future improvement is directional time-of-use (TOU) tolls (10). Finally, our paper  
12 provides detailed price elasticity estimates for monthly peak-hour and total usage patterns by  
13 vehicle type and direction, thereby enriching the limited evidence reported in several literature  
14 reviews (19-23).

## 17 **MODEL**

18 Our econometric formulation is shaped by the publicly available data. The challenge is how to best  
19 exploit these monthly data to estimate the nine vehicle types' responses to the proposed toll  
20 changes.

### 22 **Usage Data and Variable Definitions**

23 We begin by considering each tunnel's monthly total usage data by direction that corresponds to  
24 nine vehicle types, indexed herein by  $m = 1$  (private cars), 2 (taxis), 3 (motorcycles), 4 (light  
25 buses), 5 (single deck buses), 6 (double deck buses), 7 (goods vehicles not more than 5.5 tonnes), 8  
26 (goods vehicles between 5.5 and 24 tonnes), and 9 (goods vehicles over 24 tonnes). Each tunnel's  
27 peak-hour usage data by direction corresponds to three size-differentiated vehicle groups, each of  
28 which has three vehicle types. The first group contains private cars, taxis, and motorcycles, the  
29 second light buses, single deck buses, and goods vehicles not more than 5.5 tonnes, and the third  
30 double deck buses, goods vehicles between 5.5 and 24 tonnes, and goods vehicles over 24 tonnes.  
31 We derive the peak-hour usage data at the vehicle type level by allocating each group's peak-hour  
32 usage among the group's three constituent vehicle types based on each vehicle type's share of the  
33 group's monthly total usage.

34 Let  $t = 1$  for January 2003, ...,  $T = 150$  for June 2015. For a given  $t$  and specific direction  
35 (e.g., northbound), we define five usage variables for characterizing the various price elasticities.  
36 For notational simplicity, we suppress, for the time being, the subscripts used to index a usage  
37 variable's vehicle type and direction.

38 The first variable is  $N_{jt}$  = the vehicle type's monthly total usage of tunnel  $j$ . The second  
39 variable is  $M_{jt}$ , the vehicle type's usage in tunnel  $j$ 's peak hour in month  $t$ . The third variable is  $P_{jt}$   
40 = toll of tunnel  $j$  in month  $t$ . The fourth and fifth variables are  $Y_t$  = Hong Kong's monthly real GDP  
41 and  $t$  = monthly index that captures the time trend's effect on non-toll costs.

### 43 **Monthly Total Usage and Peak-Hour Usage of a Given Vehicle Type**

44 To analyze the vehicle-specific price responsiveness of  $N_{jt}$  and  $M_{jt}$ , we follow the Generalized  
45 Leontief (GL) specification in (13, 24, 25). We choose the GL specification because of its global  
46 properties as a flexible functional form in characterizing demands with low cross-price  
47 responsiveness. The resulting linear usage equations meaningfully link each vehicle type's  $N_{jt}$  and

1  $M_{jt}$ , thereby yielding transparent calculations of aggregate peak-hour and total usage responses by  
2 tunnel and direction.

3 The GL equation for vehicle type's monthly total usage,  $N_{jt}$ , in month  $t$  is:

$$4 \quad N_{jt} = \beta_{jj} + \sum_{k \neq j} \beta_{jk} (P_{kt} / P_{jt})^{1/2} + \psi_j Y_t + \phi_j t, \quad (1)$$

5 and the vehicle type's peak-hour usage of tunnel  $j$  is:

$$6 \quad M_{jt} = \alpha_{jj} + \sum_{k \neq j} \alpha_{jk} (P_{kt} / P_{jt})^{1/2} + \theta_j Y_t + \lambda_j t. \quad (2)$$

7 Equations (1) and (2) state that  $N_{jt}$  and  $M_{jt}$  linearly depends on  $(P_{kt} / P_{jt})^{1/2}$ ,  $Y_t$ , and  $t$ .  $\beta_{jj}$  and  $\alpha_{jj}$  are  
8 constants.  $\{\beta_{jk}, \alpha_{jk}\}$  for  $j \neq k$  are time-invariance coefficients. The effect of GDP on tunnel usage  
9 measured by  $\psi_j$  and  $\theta_j$  has two components: (a) rising income that tends to raise car ownership and  
10 drivers' trip requirements; and (b) rising income that tends to raise drivers' congestion costs. If (a)  
11 dominates (b), rising income tends to raise the tunnel usage.

12 The effect of the time trend on tunnel usage, measured by  $\phi_j$  and  $\lambda_j$  also has two  
13 components: (a) rising operations and maintenance and fuel costs that tend to increase the non-toll  
14 costs; and (b) an expanding transportation infrastructure (e.g., new expressways) that tends to  
15 reduce drivers' congestion costs. If (a) dominates (b), hourly tunnel usage tends to decline over  
16 time, after accounting for the effects of the monthly GDP and tunnel tolls.

## 18 Price Elasticities

19 There are four kinds of price elasticities by direction. Because of the nonlinear nature of the  
20 elasticity formulae, we use sample enumeration via a two-step procedure to perform the elasticity  
21 calculations (13).

22 The first kind is a given vehicle type's disaggregate price elasticities for monthly total  
23 usage of tunnel  $j$ . In step 1, we calculate

$$24 \quad \eta_{jit} = \partial \ln N_{jt} / \partial \ln P_{jt} = -1/2 \sum_{k \neq j} \beta_{jk} (P_{kt} / P_{jt})^{1/2} / N_{jt},$$

25 the vehicle type's own-price elasticity in month  $t$ . In step 2, we calculate  $\eta_{ij} = \sum_t \eta_{jit} / T$ , the  
26 equally-weighted average of  $\eta_{jit}$  to measure the vehicle-specific monthly total usage's average  
27 own-price responsiveness.

28 Using the same two-step procedure, we first calculate

$$29 \quad \eta_{jkt} = \partial \ln N_{jt} / \partial \ln P_{kt} = 1/2 \beta_{jk} (P_{kt} / P_{jt})^{1/2} / N_{jt} \text{ for } k \neq j,$$

30 the vehicle type's cross-price elasticity in month  $t$ . We then calculate

$$31 \quad \eta_{jk} = \sum_t \eta_{jkt} / T,$$

32 the equally-weighted average of  $\eta_{jkt}$  to measure the vehicle-specific monthly total usage's average  
33 cross-price responsiveness.

34 The second kind is tunnel  $j$ 's aggregate price elasticities, each of which is denoted by  $E_{jk} =$   
35 percentage change in tunnel  $j$ 's aggregate usage due to a one-percent change in tunnel  $k$ 's nine  
36 vehicle-specific tolls. Based on (13),  $E_{jk} = (\sum_t \sum_m \eta_{jkm} W_{jmt}) / T$ , where  $\eta_{jkm} =$  vehicle type  $m$ 's  $\eta_{jkt}$   
37 value and  $W_{jmt} =$  vehicle type  $m$ 's share of tunnel  $j$ 's aggregate usage in month  $t$ .

38 The third kind is a particular vehicle type's disaggregate price elasticities for peak-hour  
39 usage of tunnel  $j$ . The vehicle-specific peak-hour usage's own-price elasticity is

$$40 \quad \gamma_{jj} = \sum_t \gamma_{jjt} / T, \text{ where } \gamma_{jjt} = \partial \ln M_{jt} / \partial \ln P_{jt} = -1/2 \sum_{k \neq j} \alpha_{jk} (P_{kt} / P_{jt})^{1/2} / M_{jt}.$$

41 The cross-price elasticities are

$$42 \quad \gamma_{jk} = \sum_t \gamma_{jkt} / T, \text{ where } \gamma_{jkt} = \partial \ln M_{jt} / \partial \ln P_{kt} = 1/2 \alpha_{jk} (P_{kt} / P_{jt})^{1/2} / M_{jt} \text{ for } k \neq j.$$

43 The fourth kind is tunnel  $j$ 's aggregate peak-hour usage elasticities, each of which is  
44 denoted by  $A_{jk} =$  percent change in tunnel  $j$ 's aggregate peak-hour usage due to a one-percent  
45 change in tunnel  $k$ 's nine vehicle-specific tolls. Based on (13),  $A_{jk} = (\sum_t \sum_m \gamma_{jkm} S_{jmt}) / T$ , where  $\gamma_{jkm}$

1 = vehicle type  $m$ 's  $\gamma_{jkt}$  value and  $S_{jmt}$  = vehicle type  $m$ 's share of tunnel  $j$ 's aggregate peak-hour  
2 usage in month  $t$ .

3

#### 4 **Tunnel Usage Responses**

5 Let  $P_{jm}$  denote the current toll paid by the drivers of vehicle type  $m$  at tunnel  $j$ . Further, let  $P_{jm}'$   
6 denote the proposed toll. Based on equation (1), the effect of a proposed change in tolls on vehicle  
7 type  $m$ 's total usage per month of tunnel  $j$  for a given direction is:

$$8 \quad X_{jm} = \sum_{k \neq j} \beta_{jkm} [(P_{km}' / P_{jm}')^{1/2} - (P_{km} / P_{jm})^{1/2}], \quad (3)$$

9 where  $\beta_{jkm}$  = vehicle type  $m$ 's  $\beta_{jk}$  coefficient for that direction. Hence, the aggregate usage  
10 response per month by all vehicle types for tunnel  $j$  for a given direction is:

$$11 \quad X_j = \sum_m X_{jm}. \quad (4)$$

12 Based on equation (2), the effect of the proposed toll change on vehicle type  $m$ 's peak-hour  
13 usage of tunnel  $j$  is:

$$14 \quad Z_{jm} = \sum_{k \neq j} \alpha_{jkm} [(P_{km}' / P_{jm}')^{1/2} - (P_{km} / P_{jm})^{1/2}], \quad (5)$$

15 where  $\alpha_{jkm}$  = vehicle type  $m$ 's  $\alpha_{jk}$  coefficient for that direction. As there are 730 hours per month (=   
16 8760 hours per year  $\div$  12 months per year), the peak-hour response  $Z_{jm}$  equals the per hour usage  
17 response ( $X_{jm} / 730$ ) when  $\alpha_{jkm} = (\beta_{jkm} / 730)$ .

18 Finally, the aggregate peak-hour usage response by all vehicle types for tunnel  $j$  is:

$$19 \quad Z_j = \sum_m Z_{jm}. \quad (6)$$

20

#### 21 **Testable Hypotheses**

22 To better understand congestion management via directional TOU tolls, we use equations (3) and  
23 (5) to develop testable hypotheses based on linear restrictions on the GL system's coefficients  
24 associated with the square-rooted price ratios. Rejecting these hypotheses would suggest the new  
25 toll design's effectiveness is beyond what could be accomplished by the currently non-directional  
26 and time-invariant design.

27 The first hypothesis is **H1**: vehicle-type  $m$ 's per hour usage response and peak-hour usage  
28 response are equal for a given direction. Under **H1**, we have:

29 **H1A**: northbound  $(\beta_{jkm} / 730) =$  northbound  $\alpha_{jkm}$  for all  $j \neq k$ .

30 **H1B**: southbound  $(\beta_{jkm} / 730) =$  southbound  $\alpha_{jkm}$  for all  $j \neq k$ .

31 If **H1A** and **H1B** hold for *both* directions, we have:

32 **H1C**: northbound  $(\beta_{jkm} / 730) =$  northbound  $\alpha_{jkm}$  *and* southbound  $(\beta_{jkm} / 730) =$  southbound  
33  $\alpha_{jkm}$  for all  $j \neq k$ .

34 The second hypothesis is **H2**: vehicle-type  $m$ 's directional monthly total usage responses  
35 are identical. Under **H2**, northbound  $\beta_{jkm} =$  southbound  $\beta_{jkm}$  for all  $j \neq k$ .

36 The third hypothesis is **H3**: vehicle-type  $m$ 's directional peak-hour usage responses are  
37 identical. Under **H3**, northbound  $\alpha_{jkm} =$  southbound  $\alpha_{jkm}$  for all  $j \neq k$ .

38 The last hypothesis combines **H2** and **H3**, resulting in **H4**: vehicle-type  $m$ 's monthly total  
39 usage *and* peak-hour usage responses do not vary by direction. Under **H4**, northbound  $\beta_{jkm} =$   
40 southbound  $\beta_{jkm}$  *and* northbound  $\alpha_{jkm} =$  southbound  $\alpha_{jkm}$  for all  $j \neq k$ .

41

42

#### 43 **ESTIMATION STRATEGY**

44 As there are three tunnels and nine vehicle types, each direction has 54 equations (= 27 monthly  
45 total usage equations + 27 peak-hour usage equations) to be estimated. Since there are two



directions, 108 is the total number of equations to be estimated. Our estimation restricts  $\beta_{jkm} = \beta_{kjm} \geq 0$  and  $\alpha_{jkm} = \alpha_{kjm} \geq 0$  for all  $j \neq k$  and  $m$ , thus satisfying the price concavity requirement of a well-behaved cost function.

Our initial exploration reveals that we cannot jointly estimate the 108 usage equations due to the problem of non-convergence. As a result, we separately estimate each of the nine vehicle-specific GL systems to obtain its  $\alpha_{jkm}$  and  $\beta_{jkm}$  estimates. Each vehicle-specific system has 12 regressions: (a) three northbound monthly total usage regressions; (b) three southbound monthly total usage regressions; (c) three northbound peak-hour usage regressions; and (d) three southbound peak-hour usage regressions. To ascertain that our regression results are not spurious, we first examine if our sample's monthly data series have a unit root and are therefore non-stationary.

Based on the Phillips-Perron (PP) test (26), real GDP is found to be trend-stationary and the monthly total usage and peak-hour usage are either stationary or trend-stationary at the 5% significance level used throughout the rest of this paper. The monthly square-rooted toll ratios are non-stationary. These ratios' infrequent variations, however, obviate the need to remedy the apparent non-stationarity problem because they are akin to shift dummies that move tunnel usage in response to toll changes. Hence, we directly use the monthly data series to estimate the tunnel usage equations. The nine estimation samples by vehicle type are available from the corresponding author upon request.

We apply the iterative seemingly unrelated regression (ITSUR) method in (27) to estimate vehicle type  $m$ 's monthly total usage and peak-hour usage equations differentiated by tunnel and direction:

$$\text{Monthly total usage: } N_{jmt} = \beta_{jjm} + \sum_{k \neq j} \beta_{jkm} (P_{kmt} / P_{jmt})^{1/2} + \psi_{jm} Y_t + \phi_{jm} t + \nu_{jmt}, \quad (7.a)$$

$$\text{Peak-hour usage: } M_{jmt} = \alpha_{jjm} + \sum_{k \neq j} \alpha_{jkm} (P_{kmt} / P_{jmt})^{1/2} + \theta_{jm} Y_t + \lambda_{jm} t + \mu_{jmt}. \quad (7.b)$$

The estimated  $N_{jmt}$  and  $M_{jmt}$  should be positive, as required by a well-behaved cost function. This requirement is met when the coefficient estimates in equations (7.a) and (7.b) are all positive.

The random errors  $\nu_{jmt}$  and  $\mu_{jmt}$  on the right-hand-side (RHS) of equations (7.a) and (7.b) are assumed to be contemporaneously correlated and follow an AR(3) process. The errors are contemporaneously correlated because vehicle type  $m$ 's usage pattern of the three tunnels is the result of the decision making by drivers of that vehicle type (e.g., private cars, motorcycles, or goods vehicles) or passengers of that vehicle type (e.g., taxis or buses). The AR(3) assumption is based on an exploration of an AR(4) process, finding that over 90% of the fourth AR parameter estimates are insignificant. These results are available upon request.

## RESULTS

### ITSUR Regressions

The GL systems for taxis and buses have  $\alpha_{jkm}$  and  $\beta_{jkm}$  ( $j \neq k$ ) estimates that are restricted to zero. Hence, these public transportation vehicles have price-insensitive monthly total and peak-hour usage patterns, reflecting that their drivers do not have route choices and do not pay the tunnel tolls. This finding also suggests that passengers' route choices do not translate into empirically detectable price-sensitivity of tunnel usage patterns of taxis and buses.

The rest of this subsection focuses on the results of the 30 monthly total usage and 30 peak-hour usage regressions for private cars, motorcycles, and goods vehicles. Table 1 summarizes the voluminous coefficient estimates. Panel A indicates that some intercept estimates

1 are significantly negative. Thus, we use the estimated regressions to calculate the within-sample  
 2 predictions of the peak-hour and monthly total usage. These predictions are strictly positive for all  
 3 observations, as required by a well-behaved cost function.

4 Panel B reports the estimates for  $\alpha_{jkm}$  and  $\beta_{jkm}$  ( $j \neq k$ ). Ten of the 30  $\alpha_{jkm}$  estimates are  
 5 significantly positive for the peak-hour usage regressions. Twenty-two of the 30  $\beta_{jkm}$  estimates are  
 6 significantly positive for the monthly total usage regressions. While there are negative  $\alpha_{jkm}$  and  
 7  $\beta_{jkm}$  coefficient estimates, they are all insignificant and therefore restricted to zero. Hence, Panel B  
 8 suggests the empirical plausibility of the peak-hour and monthly total usage regressions for private  
 9 cars, motorcycles and goods vehicles.

10 The significant coefficient estimates for monthly GDP in Panel C suggest that rising GDP  
 11 tends to raise monthly total usage, though less so for peak-hour usage. The time trend's coefficient  
 12 estimates in Panel D have mixed significance levels and signs. Hence, they do not tell a uniform  
 13 story of how the monthly total usage and peak-hour usage may move over time, after accounting  
 14 for the effects of the tunnel tolls and monthly GDP.

### 16 Hypothesis Testing

17 The second to fourth columns of Table 2 report the  $p$ -values of the Wald statistics for testing **H1A**  
 18 to **H1C**, suggesting that the peak-hour usage and per hour usage of private cars, motorcycles, and  
 19 goods vehicles have different price sensitivities. The  $p$ -values for testing **H2** indicate that the price  
 20 sensitivity of private cars' and goods vehicles' monthly total usage varies by direction. The  
 21  $p$ -values for testing **H3**, however, suggest that the peak-hour usage's price sensitivity is largely  
 22 non-directional. The  $p$ -values for testing **H4** indicate directionally differentiated responses by  
 23 private cars and goods vehicles. When taken together, these findings suggest the potential  
 24 usefulness of directional TOU tolls to ease the CHT's congestion.

### 26 Price Elasticity Estimates

27 When calculating the price elasticities reported here and the tunnel usage responses in the next  
 28 section, we conservatively set the insignificant  $\alpha_{jkm}$  and  $\beta_{jkm}$  ( $j \neq k$ ) estimates to zero for two  
 29 reasons. First, using the unadjusted  $\alpha_{jkm}$  estimates leads to implausibly large peak-hour elasticity  
 30 estimates. Second, the response estimates given by equations (4) and (6) are insignificant when the  
 31  $\alpha_{jkm}$  and  $\beta_{jkm}$  ( $j \neq k$ ) estimates are insignificant. Setting the insignificant  $\alpha_{jkm}$  and  $\beta_{jkm}$  estimates to  
 32 zero pre-empts allegations of an imprudent use of large but insignificant response estimates to  
 33 substantiate price-management's effectiveness in easing CHT congestion.

34 Table 3 reports the own- and cross-price elasticity estimates for the monthly total usage of  
 35 private cars, motorcycles, and goods vehicles, showing that these vehicle types have  
 36 price-inelastic total usage patterns. Table 4 reports the own- and cross-price elasticity estimates for  
 37 the peak-hour usage patterns of private cars, motorcycles, and goods vehicles. These peak-hour  
 38 elasticity estimates are generally smaller in size than those in Table 3. This makes sense because  
 39 the peak-hour estimates correspond to the maximal tunnel demands of the drivers of these vehicle  
 40 types.

41 Panels A and B of Table 5 report the aggregate own- and cross-price elasticity estimates for  
 42 each tunnel's total usage, showing that all three tunnels exhibit price-inelastic usage patterns.  
 43 Panels C and D report the aggregate own- and cross-price elasticity estimates for each tunnel's  
 44 peak-hour usage. These peak-hour elasticity estimates are generally smaller in size than those in  
 45 Panels A and B.

46

## AGGREGATE RESPONSES TO THE PROPOSED TOLL CHANGES

Panel A of Table 6 presents the HKSAR Government's three options for the CHT's and EHC's toll changes (9). Some of the relative toll changes are large, as evidenced by Option A's 25% (= HK\$5/HK\$20) increase for the CHT's toll for private cars and 87% (= HK\$26/HK\$30) increase for the CHT's toll for goods vehicles over 24 tonnes.

Based on equation (4), Panel B of Table 6 summarizes each option's estimated effects on each tunnel's monthly total usage by direction. It shows that Option A is estimated to reduce the CHT's total usage by between 11.3% and 12.0% and increase the EHC's by between 14.9% and 15.1%. Its estimated effect on the WHC is negligible. The estimated effects of the other options are smaller than, but qualitatively similar to, those of Option A.

Based on equation (6), Panel C of Table 6 summarizes each option's estimated effects on each tunnel's monthly peak-hour usage by direction. It shows that Option A is estimated to reduce the CHT's peak-hour usage by about 9.6% to 16.8% and increase the EHC's by 7.2% to 12.9%. Its estimated effect on the WHC is negligible. The other options' estimated effects are smaller than Option A's.

## CONCLUSION

Using the January 2003 – June 2015 monthly peak-hour and total usage data for nine vehicle types, we document that Hong Kong can price-manage its CHT's congestion because the three cross-harbor tunnels' aggregate usage patterns are found to have discernible price responsiveness. The three tunnels' disaggregate price elasticity estimates, however, suggest price-inelastic monthly total usage patterns by vehicle type. The most price-sensitive total usage pattern belongs to motorcycles, followed by private cars and goods vehicles. Taxis and buses, which are public transportation vehicles, do not have price-sensitive monthly total usage patterns. Further, the aggregate elasticity estimates indicate that the three tunnels' monthly total usage patterns are price-inelastic, implying that the proposed toll changes can only modestly shift Hong Kong's cross-harbor tunnel traffic. Finally, the monthly peak-hour usage patterns' disaggregate and aggregate price elasticity estimates are generally smaller in size than those of the monthly total usage patterns. Hence, the effectiveness of price-managing the CHT's peak-hour congestion may be improved by implementing directional TOU tolls as part of the HKSAR Government's pilot of electronic road pricing.

## AUTHOR CONTRIBUTION STATEMENT

The authors confirm contribution to the paper as follows: study conception and design: CK Woo, KH Cao, YS Cheng; data collection: YS Cheng, KH Cao; analysis and interpretation of results: CK Woo, KH Cao, R Li; draft manuscript preparation: CK Woo, A Shiu. All authors reviewed the results and approved the final version of the manuscript.

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1 **TABLE 1 Summary of the ITSUR/AR(3) Northbound (NB) and Southbound (SB) Regressions' Coefficient**  
 2 **Estimates by Vehicle Type (m = 1, 3, 7, 8, 9) and Tunnel (j = 1, 2, 3).**

Coefficient	1. Private cars		3. Motorcycles		7. Goods vehicles not more than 5.5 tonnes		8. Goods vehicles between 5.5 and 24 tonnes		9. Goods vehicles over 24 tonnes	
	NB	SB	NB	SB	NB	SB	NB	SB	NB	SB
Panel A. Intercepts: $\alpha_{jj}$ for peak-hour usage ( $M_{jt}$ ) based on equation (2) and $\beta_{jj}$ for monthly total usage ( $N_{jt}$ ) based on equation (1)										
$\alpha_{11}$	△	▽	▼	▼	▽	△	▽	▲	▽	▲
$\alpha_{22}$	▲	▲	▼	△	△	▽	▽	△	▽	▽
$\alpha_{33}$	▲	△	▽	▽	▽	△	▽	▽	▽	▼
$\beta_{11}$	△	△	▼	▼	▼	▼	▼	▼	▽	▽
$\beta_{22}$	▽	▽	▼	▼	▼	▼	▼	▼	▼	▼
$\beta_{33}$	▼	▼	▼	▼	▼	▼	▼	▼	▼	▼
Panel B. Square-rooted toll ratios: $\alpha_{jk}$ for peak-hour usage ( $M_{jt}$ ) based on equation (2) and $\beta_{jk}$ for monthly total usage ( $N_{jt}$ ) based on equation (1)										
$\alpha_{12}$	△	▲	▲	▲	▲	▲	△	△	○	○
$\alpha_{13}$	△	△	△	▲	△	△	△	○	△	○
$\alpha_{23}$	△	○	○	○	△	△	▲	▲	▲	▲
$\beta_{12}$	▲	▲	▲	▲	▲	▲	▲	▲	△	△
$\beta_{13}$	▲	▲	▲	▲	○	▲	○	▲	△	△
$\beta_{23}$	▲	▲	△	△	▲	▲	▲	▲	▲	▲
Panel C. Monthly GDP: $\theta_j$ for peak-hour usage ( $M_{jt}$ ) based on equation (2) and $\psi_j$ for monthly total usage ( $N_{jt}$ ) based on equation (1)										
$\theta_1$	△	▽	▲	▲	▼	▽	▼	▽	▽	△
$\theta_2$	▽	▽	▲	▲	△	△	▲	▲	△	▲
$\theta_3$	△	▽	▲	▲	▲	▲	▲	▲	△	△
$\psi_1$	▲	▲	▲	▲	▲	▲	▲	▲	▲	▲
$\psi_2$	▲	▲	▲	▲	▲	▲	▲	▲	▲	▲
$\psi_3$	▲	▲	▲	▲	▲	▲	▲	▲	▲	▲
Panel D. Time trend: $\lambda_j$ for peak-hour usage ( $M_{jt}$ ) based on equation (2) and $\phi_j$ for monthly total usage ( $N_{jt}$ ) based on equation (1)										
$\lambda_1$	▽	▽	▼	▼	△	▽	△	▽	▲	△
$\lambda_2$	▽	▼	▼	▼	▼	▲	▼	▼	△	△
$\lambda_3$	▲	▲	▲	▲	▲	▲	▲	▲	▲	▲
$\phi_1$	▼	▼	▼	▼	▼	▼	▼	▼	▽	▽
$\phi_2$	▼	▼	▼	▼	▼	▼	▼	▼	▽	▽
$\phi_3$	▲	△	△	△	△	△	△	△	▲	▲

3 Notes: (1) All SAS data files, programs, output listings and logs are available from the corresponding author by  
 4 email. (2) The restrictions are  $\beta_{jk} = \beta_{kj} \geq 0$  and  $\alpha_{jk} = \alpha_{kj} \geq 0$  for all  $j \neq k$ . (3) At the 5% significance level for a  
 5 two-tailed  $t$ -test, “▲” = “positive and significant”; “▼” = “negative and significant”; “△” = “positive and  
 6 insignificant”; “▽” = “negative and insignificant”; and “○” = “negative, insignificant and restricted to zero”.

1 **TABLE 2 Summary of the  $P$ -values of the Wald Statistics for Testing H1A to H4;  $P$ -values  $\leq 0.05$  in Bold.**

Vehicle type	H1A: northbound ( $\beta_{jk} / 730$ ) = northbound $\alpha_{jk}$ for all $j \neq$ $k$ .	H1B: southbound ( $\beta_{jk} / 730$ ) = southbound $\alpha_{jk}$ for all $j \neq$ $k$ .	H1C: H1A plus H1B	H2: northbound $\beta_{jk} =$ southbound $\beta_{jk}$ for all $j \neq$ $k$ .	H3: northbound $\alpha_{jk} =$ southbound $\alpha_{jk}$ for all $j \neq$ $k$ .	H4: H2 plus H3
1. Private cars	0.7343	<b>&lt;.0001</b>	<b>&lt;.0001</b>	<b>0.0006</b>	0.6377	<b>0.0045</b>
3. Motorcycles	<b>0.0015</b>	0.0514	<b>0.0057</b>	0.0963	unavailable	unavailable
7. Goods vehicles not more than 5.5 tonnes	0.0933	0.2084	0.0972	<b>0.0048</b>	0.3416	<b>0.0075</b>
8. Goods vehicles between 5.5 and 24 tonnes	0.0757	<b>0.0340</b>	<b>0.0144</b>	<b>0.0289</b>	0.4025	0.0623
9. Goods vehicles over 24 tonnes	0.1102	<b>0.0267</b>	0.0503	0.9412	0.4953	0.7761

2 Note: PROC MODEL of SAS (2010) does not provide the  $p$ -values for **H3** and **H4** when motorcycles'  
3 northbound and southbound  $\alpha_{23}$  estimates are restricted to zero in the ITSUR/AR(3) estimation.

1 **TABLE 3 Disaggregate Elasticity ( $\eta_{jk}$ ) Estimates Based on Significant  $\beta_{jk}$  Estimates for Monthly Total Usage**  
 2 **( $N_{jt}$ ) by Direction and Vehicle Type.**

Vehicle type	$\eta_{11}$	$\eta_{12}$	$\eta_{13}$	$\eta_{21}$	$\eta_{22}$	$\eta_{23}$	$\eta_{31}$	$\eta_{32}$	$\eta_{33}$
Panel A: Northbound									
1. Private cars	-0.31	0.08	0.23	0.08	-0.32	0.24	0.17	0.18	-0.35
3. Motorcycles	-0.67	0.41	0.26	0.60	-0.60	0.00	0.88	0.00	-0.88
7. Goods vehicles not more than 5.5 tonnes	-0.32	0.32	0.00	0.32	-0.49	0.17	0.00	0.21	-0.21
8. Goods vehicles between 5.5 and 24 tonnes	-0.30	0.30	0.00	0.22	-0.41	0.19	0.00	0.28	-0.28
9. Goods vehicles over 24 tonnes	0.00	0.00	0.00	0.00	-0.53	0.53	0.00	0.88	-0.88
Panel B: Southbound									
1. Private cars	-0.35	0.10	0.24	0.11	-0.32	0.20	0.20	0.15	-0.35
3. Motorcycles	-0.63	0.39	0.24	0.60	-0.60	0.00	0.91	0.00	-0.91
7. Goods vehicles not more than 5.5 tonnes	-0.35	0.31	0.04	0.32	-0.47	0.15	0.05	0.18	-0.23
8. Goods vehicles between 5.5 and 24 tonnes	-0.32	0.27	0.05	0.21	-0.40	0.19	0.05	0.24	-0.29
9. Goods vehicles over 24 tonnes	0.00	0.00	0.00	0.00	-0.52	0.52	0.00	0.67	-0.67

3 Note: The elasticity estimates for taxis and buses are all equal to zero because their  $\beta_{jk}$  estimates ( $j \neq k$ ) have been  
 4 restricted to zero. Further, the insignificant  $\beta_{jk}$  estimates for the vehicle types in this table are conservatively set to  
 5 zero.



1 **TABLE 4 Disaggregate Elasticity ( $\gamma_{jk}$ ) Estimates Based on Significant  $\alpha_{jk}$  Estimates for Peak-Hour Usage ( $M_{jt}$ )**  
 2 **by Direction and Vehicle Type.**

Vehicle type	$\gamma_{11}$	$\gamma_{12}$	$\gamma_{13}$	$\gamma_{21}$	$\gamma_{22}$	$\gamma_{23}$	$\gamma_{31}$	$\gamma_{32}$	$\gamma_{33}$
Panel A: Northbound									
1. Private cars	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
3. Motorcycles	-0.41	0.41	0.00	0.43	-0.43	0.00	0.00	0.00	0.00
7. Goods vehicles not more than 5.5 tonnes	-1.06	1.06	0.00	0.24	-0.24	0.00	0.00	0.00	0.00
8. Goods vehicles between 5.5 and 24 tonnes	0.00	0.00	0.00	0.00	-0.23	0.23	0.00	0.32	-0.32
9. Goods vehicles over 24 tonnes	0.00	0.00	0.00	0.00	-0.56	0.56	0.00	0.91	-0.91
Panel B: Southbound									
1. Private cars	-0.21	0.21	0.00	0.13	-0.13	0.00	0.00	0.00	0.00
3. Motorcycles	-0.78	0.43	0.34	0.39	-0.39	0.00	0.71	0.00	-0.71
7. Goods vehicles not more than 5.5 tonnes	-1.16	1.16	0.00	0.37	-0.37	0.00	0.00	0.00	0.00
8. Goods vehicles between 5.5 and 24 tonnes	0.00	0.00	0.00	0.00	-0.20	0.20	0.00	0.24	-0.24
9. Goods vehicles over 24 tonnes	0.00	0.00	0.00	0.00	-0.52	0.52	0.00	0.63	-0.63

3 Note: The elasticity estimates for taxis and buses are all equal to zero because their  $\alpha_{jk}$  estimates ( $j \neq k$ ) have been  
 4 restricted to zero. Further, the insignificant  $\alpha_{jk}$  estimates for the vehicle types in this table are conservatively set to  
 5 zero.

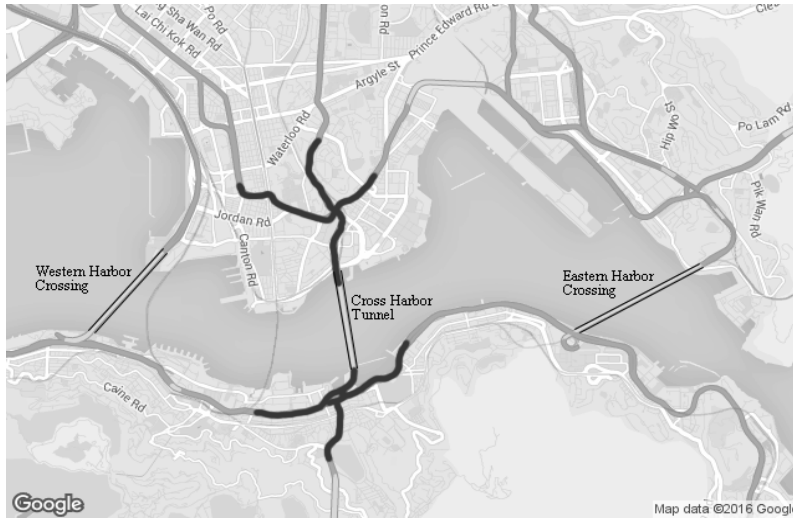
1 **TABLE 5 Aggregate Elasticity ( $E_{jk}$ ) Estimates for Monthly Total Usage and Peak-Hour Usage.**

Tunnel ID	1. Cross-Harbour Tunnel (CHT)	2. Eastern Harbour Crossing (EHC)	3. Western Harbour Crossing (WHC)
Panel A: Total Northbound Usage			
1. Cross-Harbour Tunnel (CHT)	-0.2065	0.1113	0.0951
2. Eastern Harbour Crossing (EHC)	0.1120	-0.2749	0.1629
3. Western Harbour Crossing (WHC)	0.1002	0.1179	-0.2182
Panel B: Total Southbound Usage			
1. Cross-Harbour Tunnel (CHT)	-0.2276	0.1183	0.1093
2. Eastern Harbour Crossing (EHC)	0.1313	-0.2716	0.1403
3. Western Harbour Crossing (WHC)	0.1152	0.1002	-0.2154
Panel C: Peak-Hour Northbound Usage			
1. Cross-Harbour Tunnel (CHT)	-0.1056	0.1056	0.0000
2. Eastern Harbour Crossing (EHC)	0.0503	-0.0595	0.0092
3. Western Harbour Crossing (WHC)	0.0000	0.0060	-0.0057
Panel D: Peak-Hour Southbound Usage			
1. Cross-Harbour Tunnel (CHT)	-0.2342	0.2189	0.0153
2. Eastern Harbour Crossing (EHC)	0.1313	-0.1422	0.0109
3. Western Harbour Crossing (WHC)	0.0063	0.0070	-0.0137

2

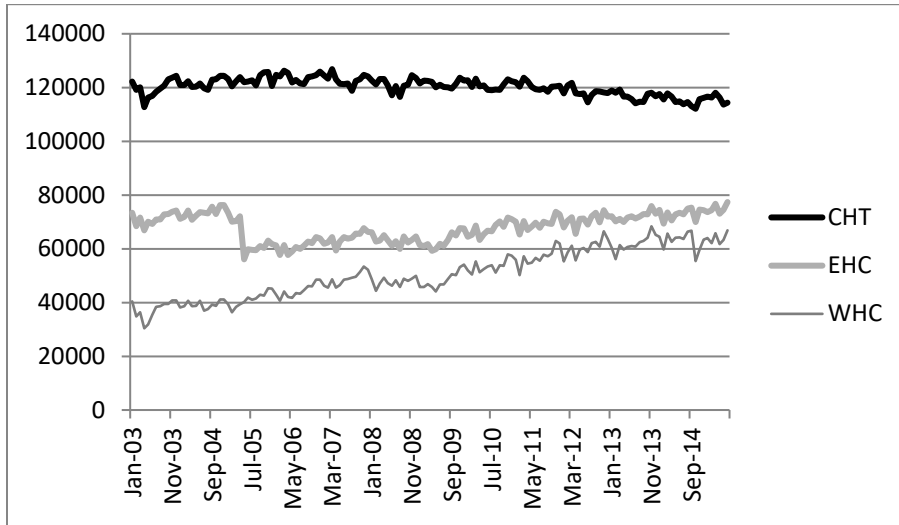
1 **TABLE 6 Aggregate Responses to the Toll Changes Proposed by the HKSAR Government.**

Vehicle type/Direction	Option A			Option B			Option C		
	CHT	EHC	WHC	CHT	EHC	WHC	CHT	EHC	WHC
Panel A: Proposed Tolls (HK\$/vehicle trip) in Hong Kong Transport and Housing Bureau (2013, p.13), with Changes from the January 2016 Tolls in ( )									
1. Private cars	25 (+5)	20 (-5)	60 (0)	25 (+5)	20 (-5)	60 (0)	30 (+10)	20(-5)	60 (0)
2. Taxis	19 (+9)	15 (-10)	55 (0)	13 (+3)	20 (-5)	55 (0)	10 (0)	15(-10)	55 (0)
3. Motorcycles	12 (+4)	9 (-4)	25 (0)	10 (+2)	10 (-3)	25 (0)	12 (+4)	9(-4)	25 (0)
4. Light buses	25 (+15)	20 (-18)	70 (0)	13 (+3)	30 (-8)	70 (0)	10 (0)	38 (0)	70 (0)
5. Single deck buses	31 (+21)	25 (-25)	110 (0)	13 (+3)	40 (-10)	110 (0)	10 (0)	50 (0)	110 (0)
6. Double deck buses	47 (+32)	38 (-37)	155 (0)	19 (+4)	60 (-15)	155 (0)	15 (0)	75 (0)	155 (0)
7. Goods vehicles not more than 5.5 tonnes	28 (+13)	23 (-15)	70 (0)	19 (+4)	30 (-8)	70 (0)	19 (+4)	23 (-15)	70 (0)
8. Goods vehicles between 5.5 and 24 tonnes	38 (+18)	30 (-20)	95 (0)	25 (+5)	40 (-10)	95 (0)	25 (+5)	30 (-20)	95 (0)
9. Goods vehicles over 24 tonnes	56 (+26)	45 (-30)	125 (0)	38 (+8)	60 (-15)	125 (0)	38 (+8)	45 (-30)	125 (0)
Panel B: Change in Average Monthly Total Usage (= Annual Sum of Monthly Total Usage ÷ 12 Months) of All Vehicle Types; Percentage Change from the July 2014 – June 2015 Value in ( )									
Northbound	-195746	171227	-4855	-129164	102324	-2015	-199055	149623	7643
	(-11.3%)	(14.9%)	(-0.5%)	(-7.4%)	(8.9%)	(-0.2%)	(-11.5%)	(13.0%)	(0.8%)
Southbound	-211428	167448	2268	-142047	102169	2878	-215854	151277	14022
	(-12.0%)	(15.1%)	(0.2%)	(-8.1%)	(9.2%)	(0.3%)	(-12.2%)	(13.6%)	(1.5%)
Panel C: Change in Average Peak-Hour Usage (= Annual Sum of Peak-Hour Usage ÷ 12 Months) of All Vehicle Types; Percentage Change from the July 2014 – June 2015 Value in ( )									
Northbound	-290	228	-7	-150	90	-3	-220	158	-7
	(-9.6%)	(7.2%)	(-0.2%)	(-5.0%)	(2.9%)	(-0.1%)	(-7.3%)	(5.0%)	(-0.2%)
Southbound	-521	414	-2	-322	229	0	-462	369	-2
	(-16.8%)	(12.9%)	(-0.1%)	(-10.3%)	(7.1%)	(-0.0%)	(-14.9%)	(11.5%)	(-0.1%)



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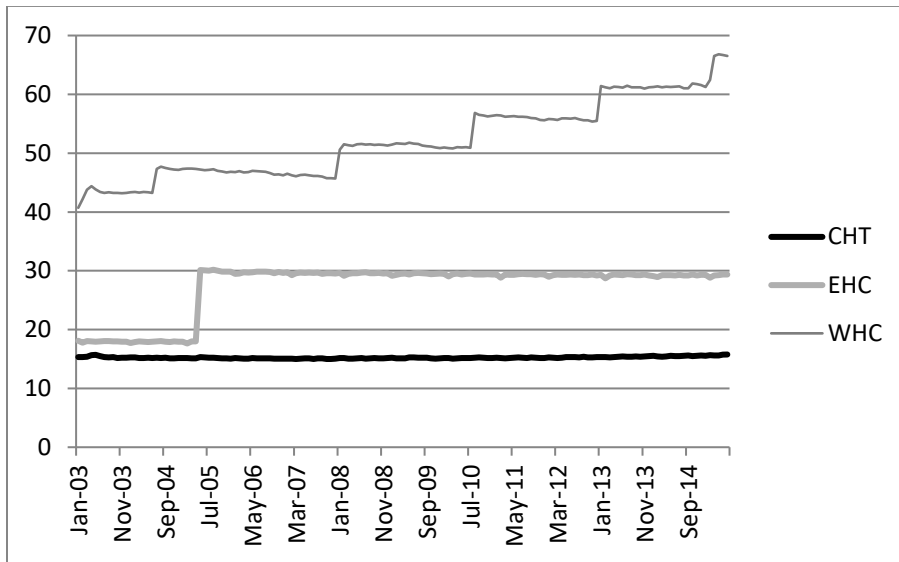
**FIGURE 1 Severe congestion at Hong Kong’s Cross-Harbour Tunnel (CHT), with the darkened line denoting the daily queues observed during rush hours along the roads leading to the CHT’s northern end in Kowloon Peninsula and southern end on Hong Kong Island (8).**



1

2 **FIGURE 2 Monthly usage of the Cross-Harbour Tunnel (CHT), Eastern Harbour Crossing**  
3 **(EHC), and Western Harbour Crossing (WHC) for January 2003 – June 2015.**

1



2

3 **FIGURE 3 Monthly average tolls in HK\$ (US\$1 ≈ HK\$7.8) of the Cross-Harbour Tunnel**  
 4 **(CHT), Eastern Harbour Crossing (EHC) and Western Harbour Crossing (WHC) for**  
 5 **January 2003 – June 2015.**